

Searches for hybrid mesons

- **Expectations for hybrid mesons**
- **Exotic quantum numbers ($J^{PC} = 1^{-+}$)**

Diffraction:

$$\pi^- N \rightarrow \eta \pi^- N$$

$$\pi^- N \rightarrow \eta' \pi^- N$$

$$\pi^- N \rightarrow b_1 \pi N$$

$$\pi^- N \rightarrow \rho^0 \pi^- N$$

$$\pi^- N \rightarrow \eta \pi^- \pi^+ N$$

Charge exchange:

$$\pi^- p \rightarrow \eta \pi^0 n$$

$$\pi^- p \rightarrow \eta' \pi^0 n$$

- **Features of π (1800)**

Expectations for hybrid mesons

$q \bar{q}$
normal
mesons

$q \bar{q} + \text{SU}(3)_f$ singlet
hybrids

$q \bar{q}$ mesons:

$$P=(-1)^{L+1} \quad C=(-1)^{L+S} \quad J^{PC} = 0^{-+}, 1^{-+}, 0^{++}, 1^{++}, 2^{++}, 1^{+-} \dots\dots\dots$$

Hybrid mesons can have exotic quantum numbers (Okun', Vainshtein 76)

$$J^{PC}_{\text{exotics}} = 1^{-+} \quad 0^{+-} \quad 2^{+-} \quad 0^{-+} \quad \dots\dots\dots$$

Smoking gun:

$$J^{PC} = 1^{-+} : \quad \pi_1$$

$$J^{PC} = 0^{-+} : \quad \pi(1800)$$

Model predictions for hybrid mesons

Hybrids were studied in:

Potential models, Bag models, Flux tube model, QCD sum rules, Lattice QCD.

As a rule models predict that exotic hybrid resonance π_1 does exist.

Prediction for mass: $M(\pi_1) = 1.6 \div 2.1 \text{ GeV}$

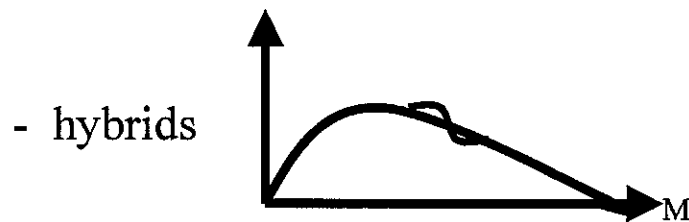
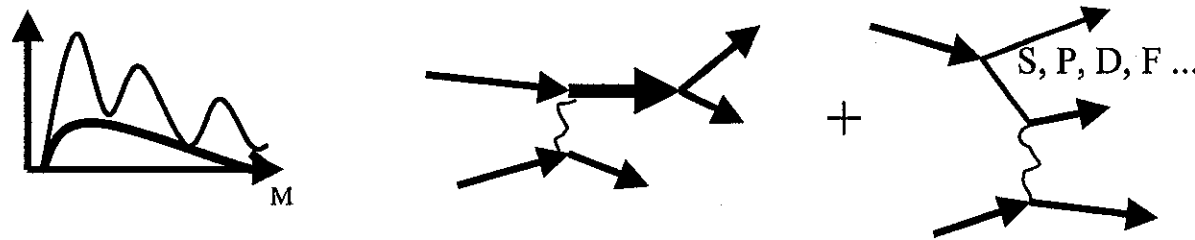
Specific prediction of QCD sum rules: $M(\pi_1') - M(\pi_1) \approx 0.2 \text{ GeV}$

Predictions for decay widths are very model dependent:

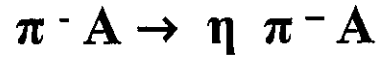
- $\eta' \pi, \eta \pi$ $A^2(\pi_1 \rightarrow \eta' \pi) / A^2(\pi_1 \rightarrow \eta \pi) = 1/\tan^2 \theta_{PS}$ {Close&Lipkin}
 $\Gamma(\pi_1(1600) \rightarrow \eta' \pi) \approx 3 \text{ MeV}$ {Narison,99}
 $\Gamma(\pi_1(1600) \rightarrow \eta \pi) \approx 1 \text{ GeV}$ {Frere}
- $\rho \pi$ $\Gamma(\pi_1(1600) \rightarrow \rho \pi) = 2 \div 8 \text{ MeV}$ {Kokoski,Page}
 $\Gamma(\pi_1(1600) \rightarrow \rho \pi) = 10 \div 100 \text{ MeV}$ {Viron}
 $\Gamma(\pi_1(1600) \rightarrow \rho \pi) = 0.6 \text{ GeV}$ {Narison}
- $b_1 \pi$ $\Gamma(\pi_1(1600) \rightarrow b_1 \pi) = 50 \div 200 \text{ MeV}$ {Iddir,Page}
- $f_1 \pi$ $\Gamma(\pi_1(1600) \rightarrow f_1 \pi) = 10 \div 50 \text{ MeV}$

Methods of hunting, problems

- search for “additional” states with normal quantum numbers
- search for “unusual” decays (suppression of decays to states with identical space wave functions, decays to $\{8\} + \{1\}$)
- search for mesons with exotic quantum numbers
- **Main problem – large nonresonance background.**
 - normal mesons:



The wave $J^{PC}=1^{-+}$ in diffractive reactions



VES, 1993, $P_\pi = 37$ GeV (confirmed by BNL)

2000, $P_\pi = 28$ GeV

The amplitude depends on 5 variables:

$s, t, M_{\eta\pi}, \theta, \varphi$

Assuming full coherency at fixed $s, t,$

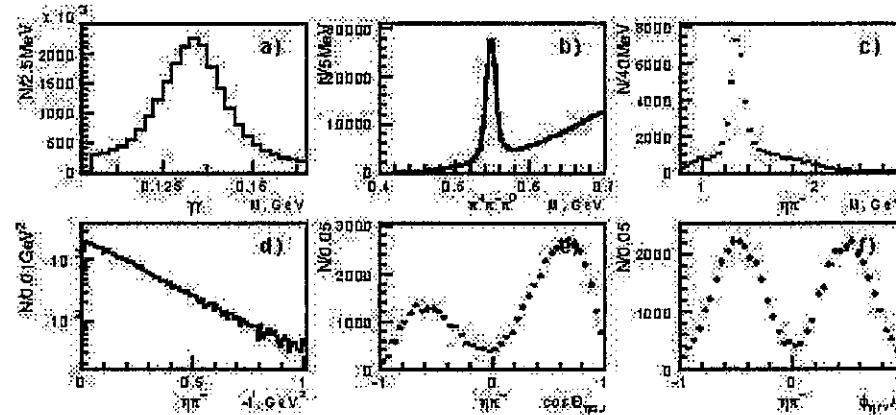
$M_{\eta\pi}$ the intensity could be written as:

$$I(\Omega) = |\sum_{J,M} a_{M-}^J F_{M-}^J|^2 +$$

$$|\sum_{J,M} a_{M+}^J F_{M+}^J|^2$$

$$F_{M\eta}^J(\Omega) = Y_M^J(\Omega) - \eta (-1)^M Y_{-M}^J(\Omega)$$

(η – “naturalness”)

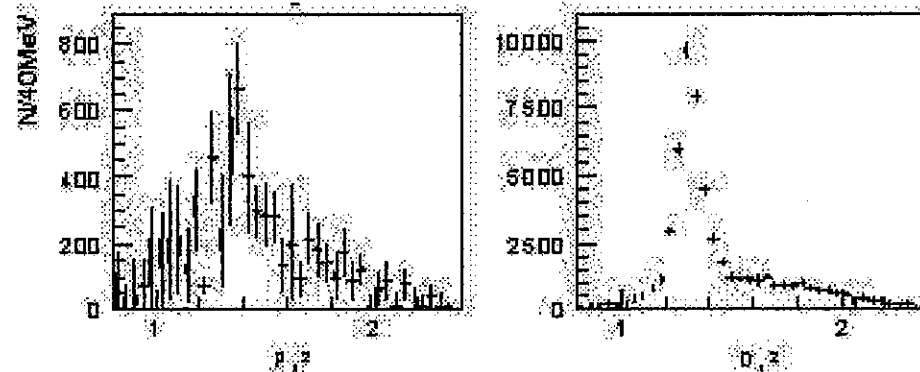


Seven waves:

$S_0, P_0, P-, D_0, D-; P+, D+$

The wave $D+$ dominates: $a_2(1320)$ and broad signal at $m > 1.4$ GeV

The wave $P+$ is clearly seen. This wave does not demonstrate narrow structures.



$$\pi^- A \rightarrow \eta \pi^- A$$

Mass-dependent fit of D+ and P+ waves in $\eta \pi$

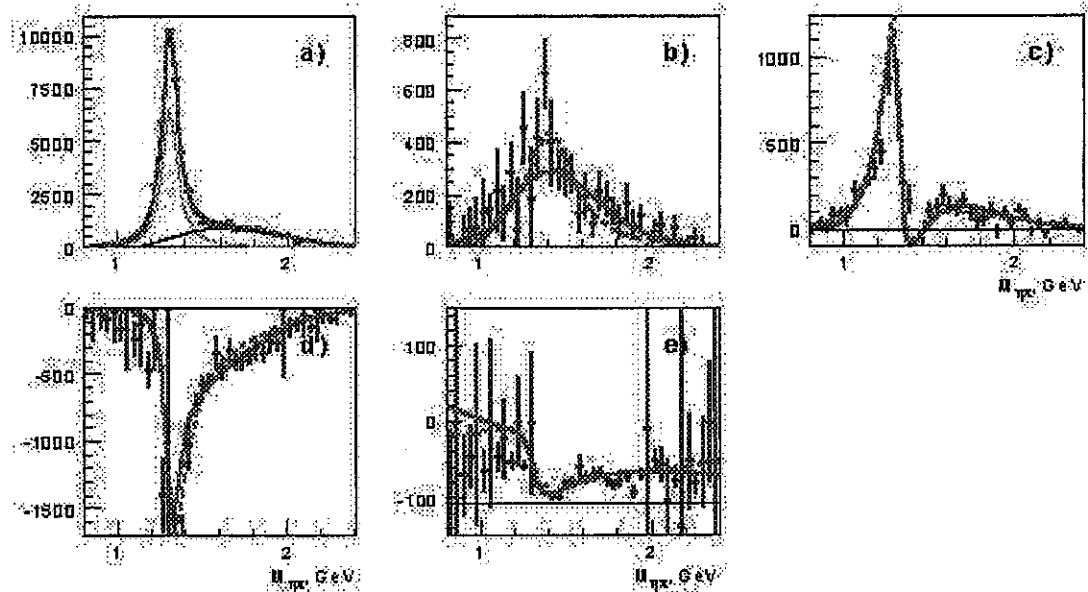
a) Intensity D+

b) Intensity P+

c) Real part of
interference term

d) Imaginary part of
interference term

e) Relative phase D+/P+



The results are fitted **equally well** by **broad resonance** in P+,
as well as by **background** with constant phase.

Summary on exotic wave $I^G J^{PC} = 1-1^{-+}$ at $M=1.4$ GeV

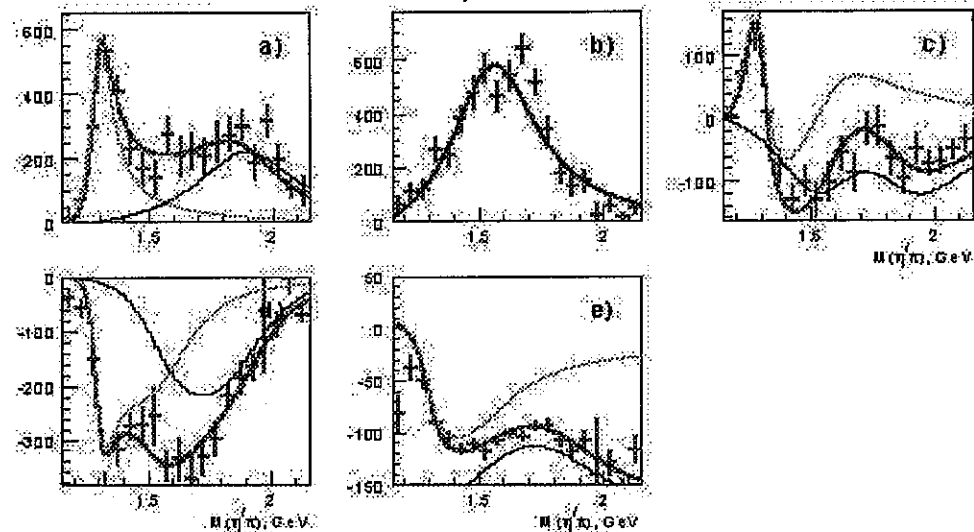
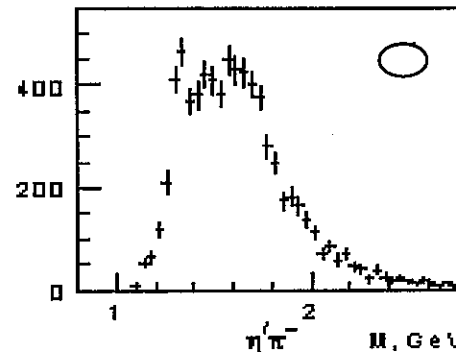
- 1. GAMS 1988 $\pi^- p \rightarrow \eta \pi^0 n$ ~~$M=1406 \pm 20$ MeV $\Gamma=180 \pm 20$ MeV~~
 - 2. KEK 1993 $\pi^- p \rightarrow \eta \pi^- p$ $M=1323 \pm 5$ MeV $\Gamma=143 \pm 12$ MeV
 - 3. VES 1993 $\pi^- N \rightarrow \eta \pi^- N$ Broad signal at $M=1.4$ GeV
 - 4. E-852 1997 $\pi^- p \rightarrow \eta \pi^- p$ $M=1370 \pm 60$ MeV $\Gamma=380 \pm 90$ MeV
 - 5. CB 1998 $n p \rightarrow \eta \pi^- \pi^0$ $M=1400 \pm 30$ MeV $\Gamma=310 \pm 90$ MeV
 - 6. GAMS 1998 $\pi^- p \rightarrow \eta \pi^0 n$ • Broad signal without BW phase
 - 7. GAMS 1999 $\pi^- p \rightarrow \eta \pi^0 n$ Mass dependent fit without resonance
 - 8. E-852 2003 $\pi^- p \rightarrow \eta \pi^0 n$
- **Main problems:** relative phase of 1^{-+} and 2^{++} waves is unmeasurable
 - the phase of 2^{++} wave is not known at $M > 1.45$ GeV
 - different experiments give very different results
 - the signal looks like ordinary nonresonant background
 - **Conclusion: experimental results do not lead to unambiguous conclusion on the existence of exotic resonance at $M \approx 1.4$ GeV**

$\pi^- A \rightarrow \eta' \pi^- A$
PWA and mass-dependent fit of D+ and P+ waves in $\eta' \pi^-$

Two signals are clearly seen:
 - the decay $a_2 \rightarrow \eta' \pi^-$
 (VES, 1992)
 - large signal in exotic wave
P+ at $M(\eta' \pi^-) \approx 1.6$ GeV.
 This result was confirmed by E852 recently.

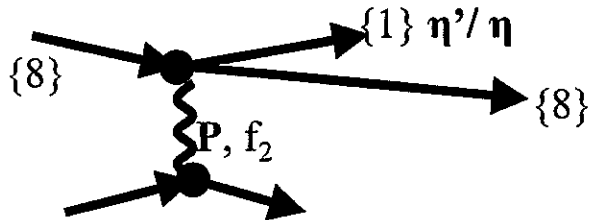
The results are fitted equally well/bad by broad resonance in **P+**, as well as by background with constant phase.

More complicated model is needed to describe possible fine structure at $M \approx 1.6-1.8$ GeV

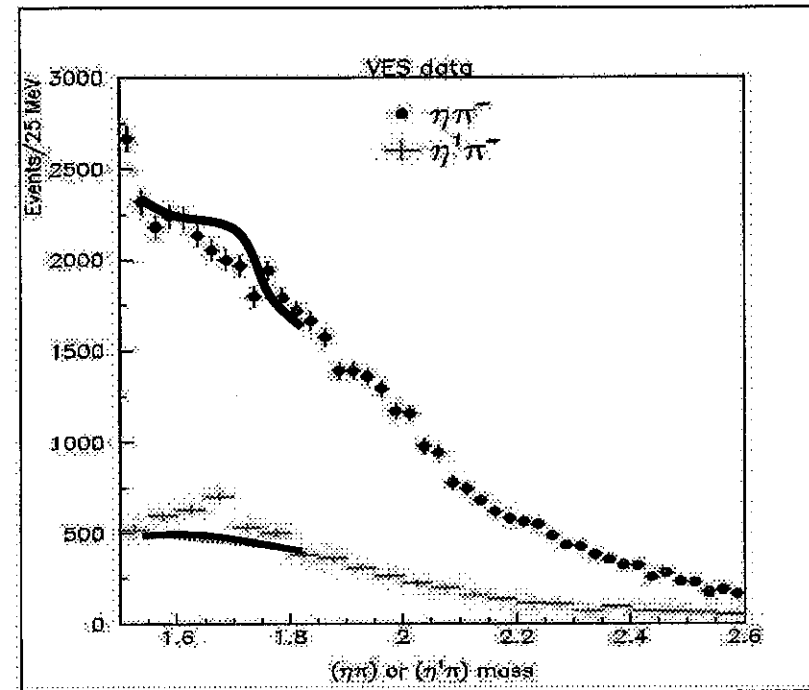


Comparison of $\eta \pi^-$ and $\eta' \pi^-$

The diffractive-like production of $\eta \pi^-$ and $\eta' \pi^-$ in P-wave is described by one amplitude:



Therefore one and the same P-wave resonance has to be seen in $\eta \pi^-$ and $\eta' \pi^-$.



We do not see statistically significant structures in $\eta \pi^-$ P-wave around $M \approx 1.6$ GeV. To make analysis less model-dependent we can look at mass-spectra without PWA and sum-up all VES runs to increase statistics. The signal expected in $\eta \pi^-$ is shown by **red** curve. This signal is not seen in the $\eta \pi^-$ mass-spectrum. Possible irregularities at 1.75 GeV and 1.85 GeV have pure statistical significance.

The reaction $\pi^- A \rightarrow b_1 \pi A$

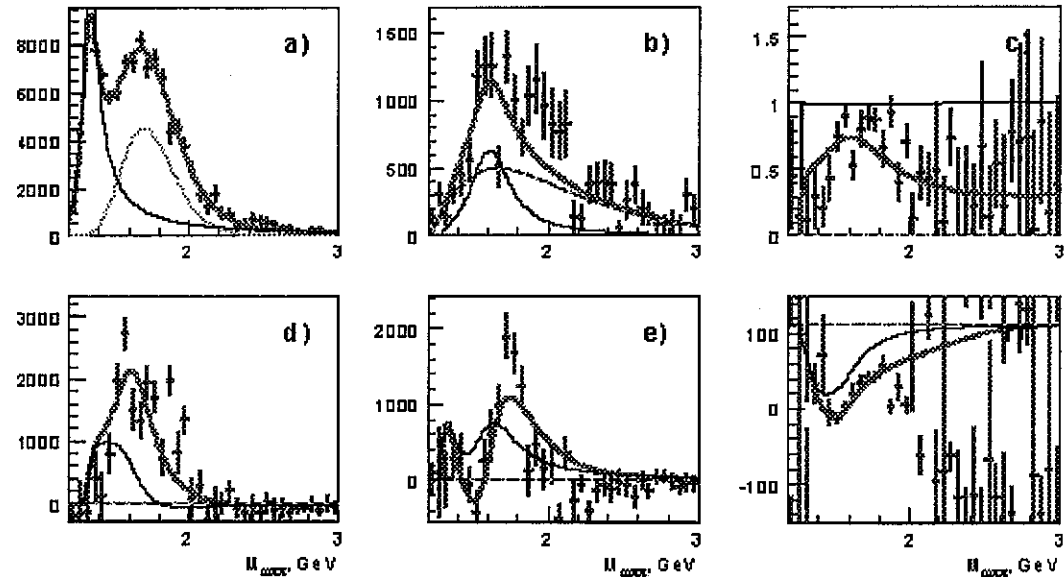
VES, 1997, $P_\pi = 37$ GeV

2000 г, $P_\pi = 28$ GeV

The reaction under study is $\pi^- A \rightarrow \pi^+ \pi^- \pi^0 \pi^0 A$

The resonance $b_1(1235)$ was selected in the channel $\omega(\pi^+ \pi^- \pi^0) \pi$

- a) Intensity D+
- b) Intensity P+
- c) Coherency D+ P+
- d) Real part of interference term D+ P+
- e) Imaginary part of interference term D+ P+
- f) Relative phase D+ / P+



D+ wave: $a_2(1320)$ and broad bump at $M=1.7$ GeV

P+ wave: broad irregular structure. Rapid variation of $\text{Im}(D+/P+)$ points to possible resonance at $M=1.6 \div 1.8$ GeV

The reaction $\pi^- A \rightarrow f_1 \pi^- A$

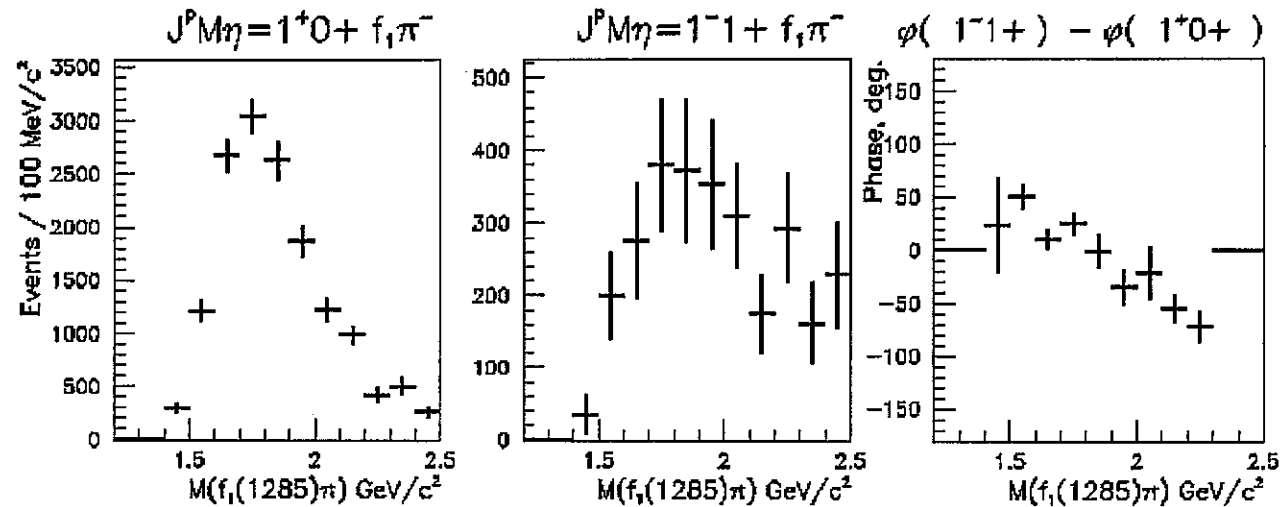
VES, 1995, $P_\pi = 37$ GeV

2002, $P_\pi = 28$ GeV

The reaction under study is: $\pi^- A \rightarrow \pi^+ \pi^- \pi^- \eta A$

The resonance $f_1(1285)$ was selected in the channel $\eta \pi^+ \pi^-$

- a) Intensity of D^+
- b) Intensity of P^+
- c) Relative phase P^+/D^+



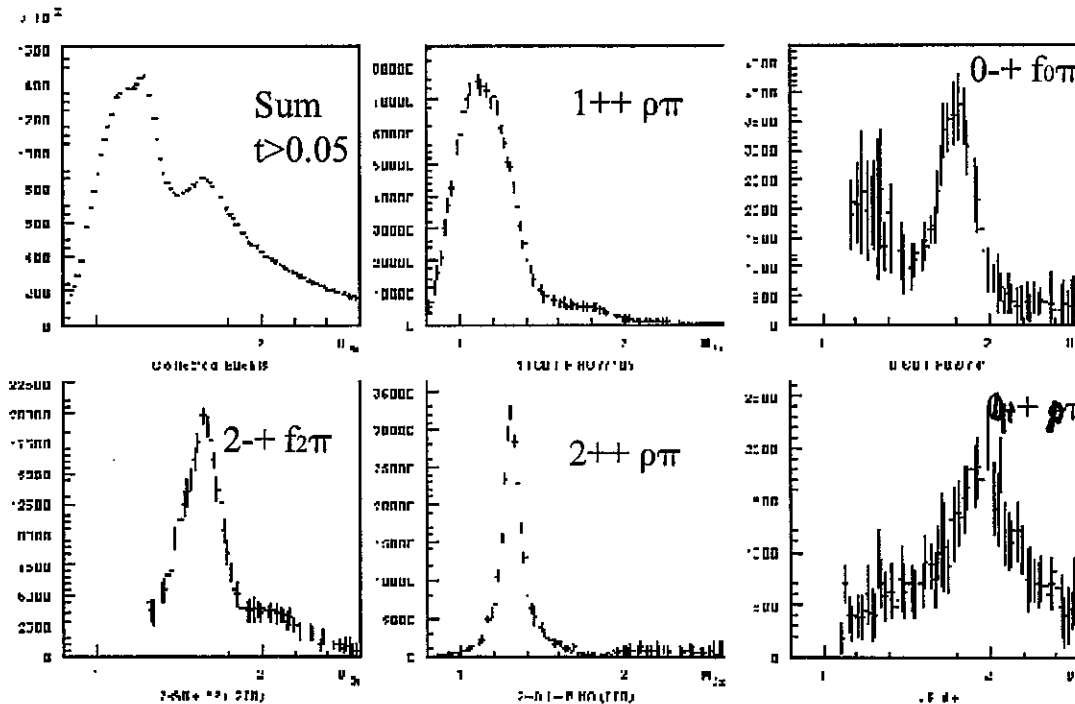
Most intensive wave $J^P M \eta = 1^+ 0^+$ has maximum at $M = 1.7$ GeV

No indication to resonances in exotic wave $J^{PC} M \eta = 1^- 1^+$.

The reaction $\pi^- A \rightarrow \pi^+ \pi^- \pi^- A$

VES, 1995, $P_\pi = 37$ GeV

2000, $P_\pi = 28$ GeV



Clear resonances are seen in waves: $J^{PC} = 1^{++}, 2^{++}, 2^{-+}, 0^{-+}, 4^{++}$

Broad exotic wave $\mathbf{1}^G(J^{PC}) = \mathbf{1}^-(1^+)$ is clearly seen in the channel $\rho\pi$ with very low intensity $\sim 2\%$ of the a_2 signal (next slide).

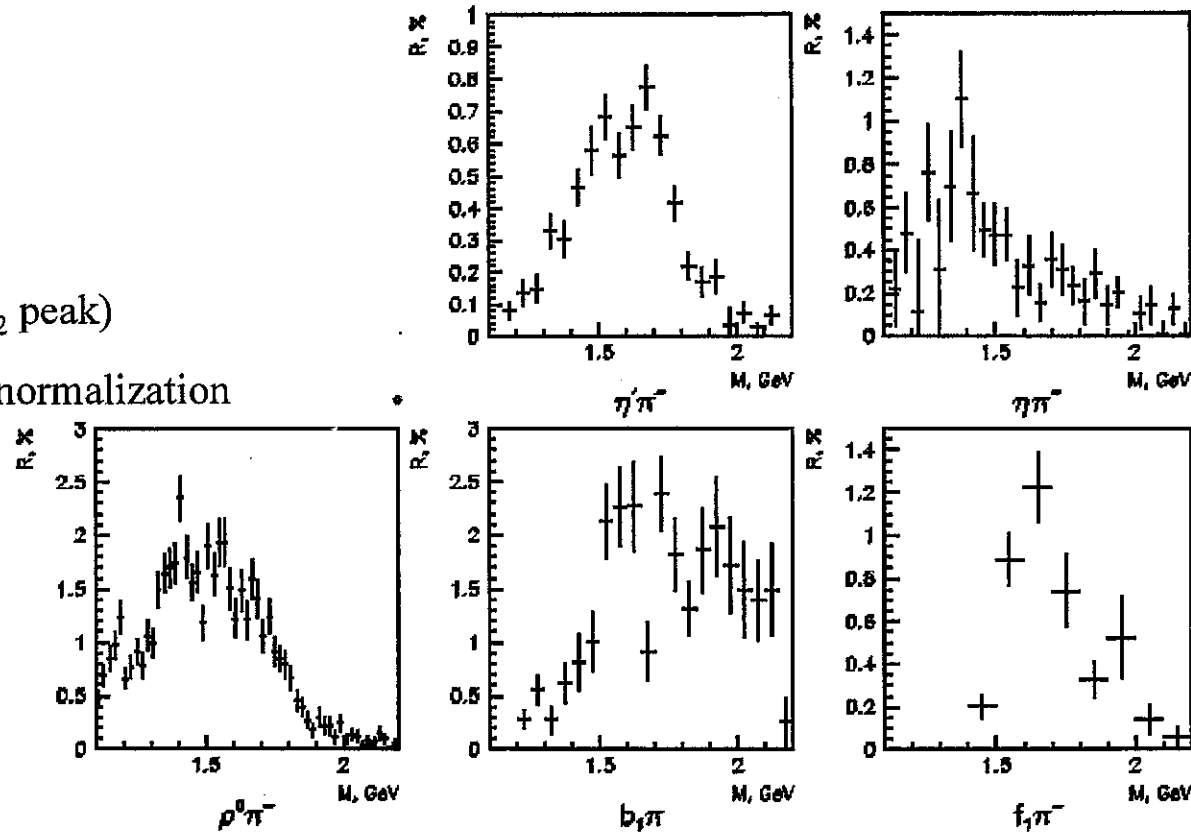
No evidence of narrow resonance at $M \approx 1.6$ GeV (difference with E852).

Conclusion on $J^{PC}=1^{-+}$ in diffractive reactions

Normalization:

$$dN(X) / dM \quad / \quad dN/dM(a_2 \text{ peak})$$

30% systematic error in normalization



Exotic wave $I^G(J^{PC})=1^-(1^+)$ is clearly seen in a number of reactions. There are indications on the existence of exotic resonance in the channel $b_1 \pi$ (and probably in $\eta' \pi^-$) at $M=1.6 \div 1.8$ GeV

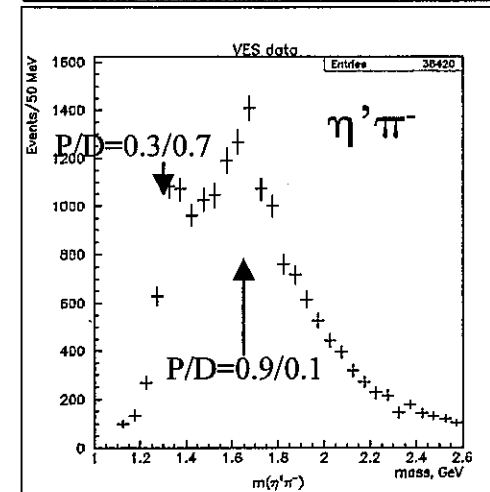
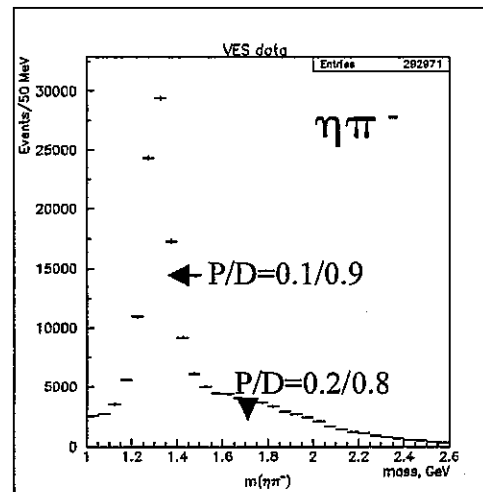
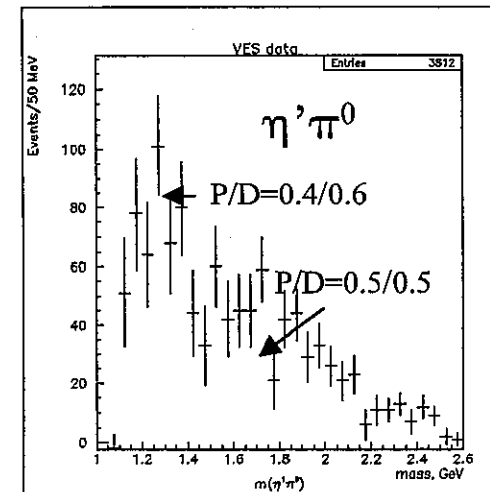
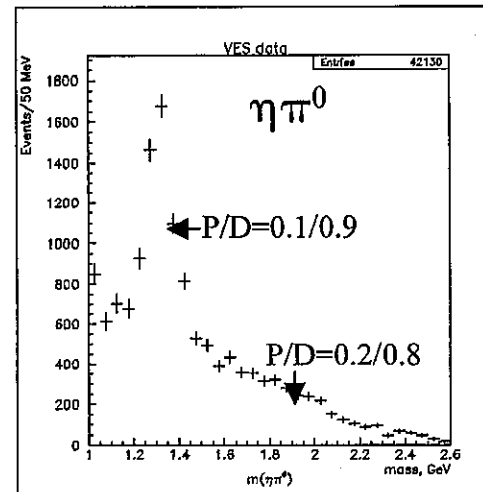
Charge exchange reactions

VES, 2003, preliminary

Comparison of charge exchange and diffractive reactions shows that mass-spectra of all four reactions are very different. The most spectacular difference is between $\eta'\pi^0$ and $\eta'\pi^-$.

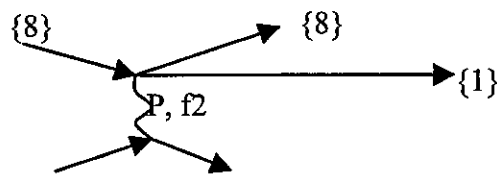
Question:
why bump at 1.65 GeV
is not seen in $\eta'\pi^0$?

Answer:
P-wave in $\eta'\pi^0$ is not
 $SU(3)_f$ -singlet, it is four-
quark state (next slide).

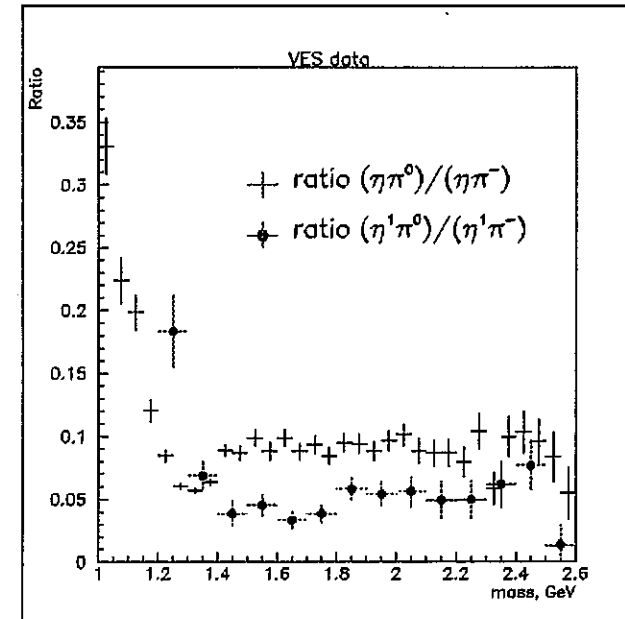


SU(3)_f structure of J^{PC}=1⁻⁺ waves in η'π and ηπ channels

It follows from SU(3)_f-symmetry that in diffractive-like reactions only one P-wave amplitude is allowed: {8}+{1} → {8}+{1}



Therefore in these reactions the ratio of P-wave amplitudes is expected as : $R=A(\eta'\pi)/A(\eta\pi) = 1/\text{tg}(\theta)_{\text{PS}}$. Experiments confirm this prediction. It does not depend whether P-wave is resonant or not.



In case of charge exchange reactions the SU(3)_f-symmetry allows P-wave amplitudes with two octets in final state ({8}+{8}). Hybrid (SU(3)_f-octet) can not decay to two octets in P-wave contrary to four-quark states, which can do it ({10}, {27}).

Experimental data show that for charge exchange reactions the P-wave in η'π⁰-channel is suppressed, therefore **multiquark states ({10}, {27}) are dominating in η'π⁰ P-wave.**

Features of $\pi(1800)$

Is it nonexotic hybrid?

The resonance $\pi(1800)$ is seen in following channels:

$f_0(980)\pi$, $\varepsilon\pi$, $a_0\eta$, $f_0(1500)\pi$.

Probably the same signal is seen in $\omega\rho$.

It is suppressed in $\rho\pi$ и K^*K .

(VES, 1993-1999)

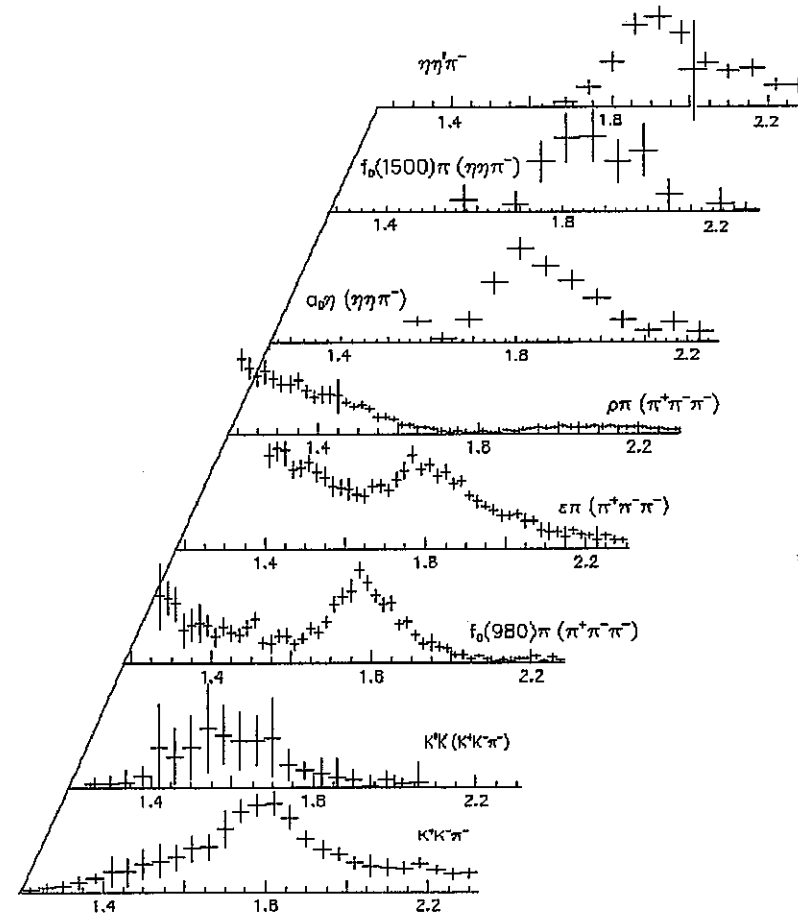
$\pi(1800)$: hybrid?

3^1S_0 ?

$K^*K^{\bar{}}$ molecule ?

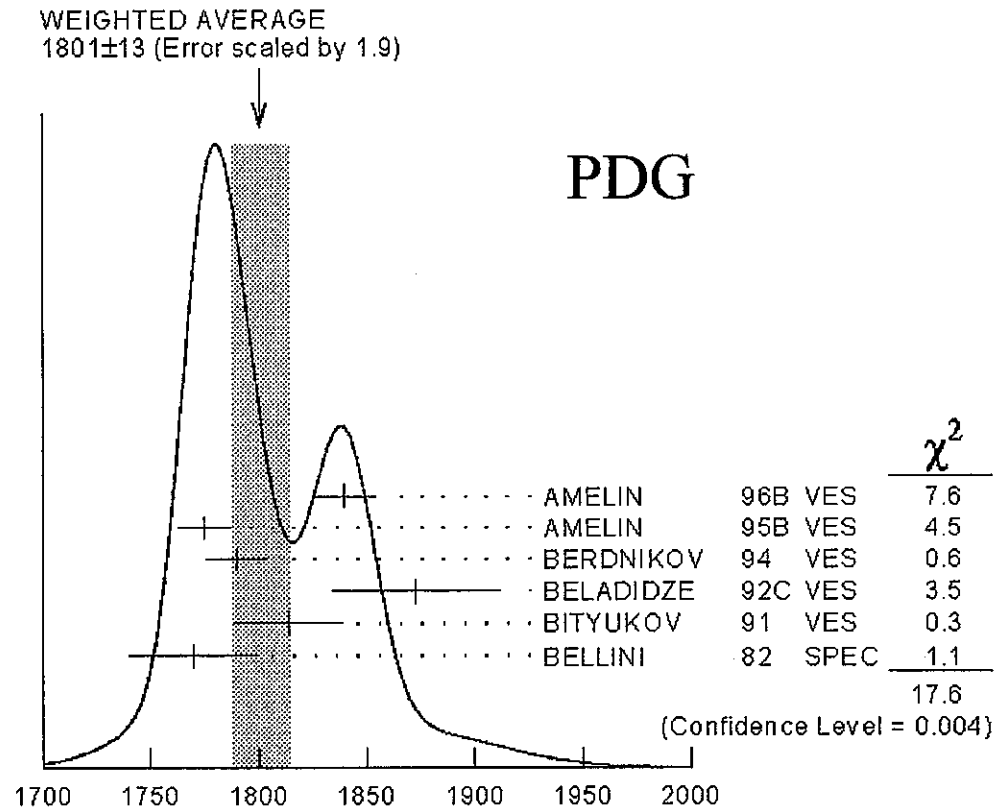
Main features:

- suppression of decays to V P (hybrids in FT model, 3^1S_0)
- decay to $f_0(1500)\pi$ (hybrids)
- abnormally high branching to $f_0(980)\pi$ (???)



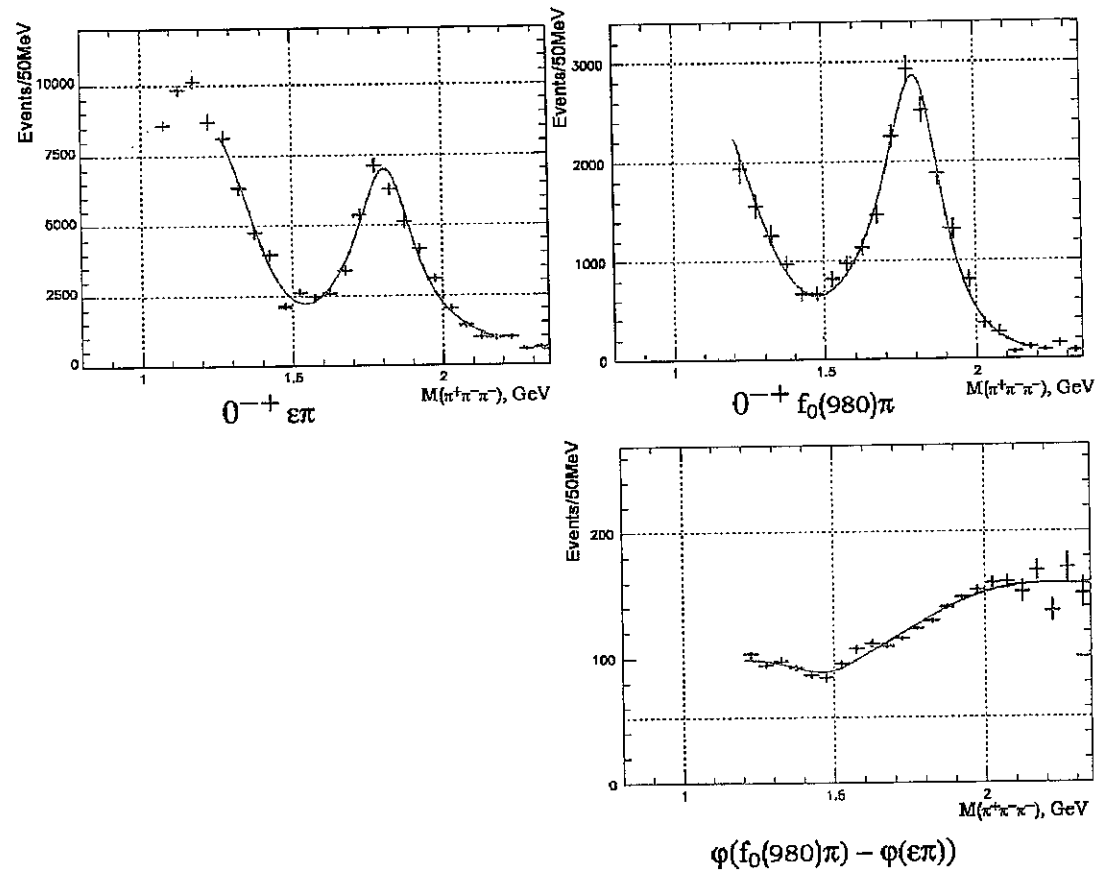
One resonance or more?

Spread of $M(\pi(1800))$
from one decay channels
to another one points to
possible existence of two
different 0^{-+} states.



The reaction $\pi^- \Lambda \rightarrow \pi^+ \pi^- \pi^- \Lambda$

VES, 1997, $P_\pi = 37$ GeV

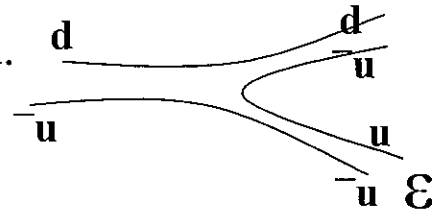


The f_0 / ε puzzle

It is expected that for conventional hybrids ($I^{GJPC}=1-0^{-+}$) as well as for second radial excitations of pion (3^1S_0) the decay $\pi(1800) \rightarrow f_0(980) \pi$ is suppressed in comparison to $\pi(1800) \rightarrow \varepsilon \pi$ (here ε is broad $\pi \pi$ S-wave object describing $f_0(600)+f_0(1370)$).

The reason is that $f_0(980)$ is coupled to strange quarks, it's narrow, the ε is coupled to u,d quarks, it's broad.

$$\text{VES: } \text{BR}(\pi(1800) \rightarrow f_0(980) \pi) \approx \frac{\text{BR}(\pi(1800) \rightarrow \varepsilon \pi)}{\dots}$$



This puzzle could be resolved assuming that these decays proceed via **emission of $SU(3)_f$ singlet** instead of tube/string breaking. The state

$f_0\{1\} \approx 1/\sqrt{2} (\varepsilon + f_0(980))$ looks like $SU(3)_f$ singlet.

Decay $\pi(1800) \rightarrow \{1\} + \{8\}$ is natural one if $\pi(1800)$ “consists of” $\bar{q} q$ (in 1S_0 state?) **and (scalar?) $SU(3)_f$ singlet excitation** (“glue”, “bag”, longitudinal excitation of flux tube etc)

Conclusions

- Exotic wave $J^{PC} = 1^{-+}$ is seen in a number of reactions
- Broad bump at $M=1.4$ GeV in $\eta\pi$ could be described equally well with or without resonance
- There are some indications on exotic resonance $J^{PC} = 1^{-+}$ in $\eta'\pi$ and $b_1\pi$ at $M= 1.7 \div 1.8$ GeV
- Charge exchange reactions with $J^{PC} = 1^{-+}$ in $\eta\pi$ and $\eta'\pi$ channels proceed via multiquark intermediate states
- Features of the $\pi(1800)$ decays point to possible existence of new excitations in hadrons (scalar, $SU(3)_f$ -singlet)